

Midterm I

Name:

SID:

- Try to answer all questions. Not all parts of a problem are weighted equally. Before you answer any question, read the problem carefully. Be precise and concise in your answers.
- You may consult at most *10 sheets of notes*. Apart from that, you may not look at books, notes, etc. Calculators, phones, computers, and other electronic devices are **NOT** permitted for looking up content. However, you may use an electronic device such as a tablet for writing your answers.
- You have 80 minutes: there are 5 questions on this exam worth a total of 100 points.
- You are allocated 90 minutes and the extra 10 minutes are provided for the submission of the exam on Gradescope. You must submit/upload the exam on time. Note that late submissions will not be accepted.
- **DSP Students** must submit the exam in time as per your accommodation. Thus, if you are allowed $1.5\times$ (resp., $2\times$) the exam time then you must submit it within $80 * 1.5 + 10$ (resp., $80 * 2 + 10$) mins, i.e. 130 (resp., 170) mins. Please make your submission via email to both sanjamg@berkeley.edu and yinuo@berkeley.edu using the subject “CS 171: Midterm 1 DSP Submission.”
- The exam must be submitted before 8 PM PT on Feb 22nd, 2021. No exams later than this time will be accepted regardless of when you start the test.
- We will not be answering questions during the exam. If you feel that something is unclear please write a note in your answer.

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1 True/False (20 points)

Bubble in the right answer. No explanation needed. +2 points for correct answer and -1 points for wrong answers! If you leave a question unanswered, then there is no penalty. This part will be graded automatically. Please mark your answer clearly.

1. Let $f : \{0, 1\}^n \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ be a pseudorandom function. Then, $f'_k(x, y) = f_k(x) \parallel x \oplus f_k(y)$ is a pseudorandom function.

True

False

2.

$$f(n) = \begin{cases} 2^{-\log^2 n} & n \text{ is odd} \\ 2^{-n} & n \text{ is even} \end{cases}$$

is a non-negligible function.

True

False

3. Consider an encryption scheme where ciphertexts contain no information about the secret key. Then, the scheme must be CPA-secure.

True

False

4. A mult-secure encryption scheme is also CPA-secure.

True

False

5. Consider a variant of the mult security definition called mult-(+1) where the adversary is additionally allowed a single phase-2 encryption query. Any encryption scheme that is mult secure is also mult-(+1) secure.

True

False

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6. The number of permutations from $\{0, 1\}^n$ to $\{0, 1\}^n$ is $(2^n)!$.
- True
- False
7. There exists a perfectly secure encryption scheme such that $\text{Enc}(k, m) = m$ with non-zero probability.
- True
- False
8. Let $g : \{0, 1\}^\ell \rightarrow \{0, 1\}^m, f : \{0, 1\}^m \rightarrow \{0, 1\}^n$ be two functions such that one of them is a pseudorandom generator. Then, $f(g(\cdot))$ is a pseudorandom generator.
- True
- False
9. Let $g_k : \{0, 1\}^\ell \rightarrow \{0, 1\}^\ell, f_s : \{0, 1\}^\ell \rightarrow \{0, 1\}^\ell$ be two functions such that one of them is a pseudorandom function and the other one is a permutation (i.e., a bijective function). Then, $f_s(g_k(\cdot))$ is a pseudorandom function.
- True
- False
10. Let $g_k : \{0, 1\}^\ell \rightarrow \{0, 1\}^m$ be a pseudorandom function and $f : \{0, 1\}^m \rightarrow \{0, 1\}^n$ be a pseudorandom generator. Then, $f(g_k(\cdot))$ is a pseudorandom function.
- True
- False

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2 Pseudorandom Generators (25 points)

Let $g : \{0, 1\}^n \rightarrow \{0, 1\}^{n+1}$ be a pseudorandom generator with stretch 1 (that is, its output is 1 bit longer than its seed). We will show how to construct from g a PRG $f : \{0, 1\}^n \rightarrow \{0, 1\}^{n+2}$ with stretch 2. First, we will show an insecure attempt at expanding the stretch, and then you will be asked to demonstrate a secure method of expanding the stretch.

1. Consider the following attempt at defining f . On input seed $s \in \{0, 1\}^n$, f computes $t := g(s)$ and then outputs $(t_1, g(t_{1,\dots,n})) \in \{0, 1\}^{n+2}$, where t_1 is the first bit of t , and $t_{1,\dots,n}$ are the first n bits of t . We will construct a PRG g for which f as defined above is **not** a PRG.
 - (a) Using a PRG $h : \{0, 1\}^{n-1} \rightarrow \{0, 1\}^n$, construct a $g : \{0, 1\}^n \rightarrow \{0, 1\}^{n+1}$ for which f as defined above is not secure. Below, write a description of g , and argue that the resulting f is not a secure PRG. (5 points)
 - (b) Prove that the g you specified above is a secure PRG, assuming that h is a secure PRG. (5 points)
2. Now, assuming that $g : \{0, 1\}^n \rightarrow \{0, 1\}^{n+1}$ is a PRG, define and prove the security of a PRG $f : \{0, 1\}^n \rightarrow \{0, 1\}^{n+2}$. (15 points)

3 CPA Security (20 points)

Consider the following variants of CPA security. Weak-1-CPA is the same as CPA security, except that the adversary is only allowed exactly 1 phase-1 query. Weak-2-CPA is the same as CPA security, except that the adversary is only allowed exactly 2 phase-1 queries. Assuming the existence of a CPA-secure scheme $(\text{Gen}, \text{Enc}, \text{Dec})$, construct a scheme $(\text{Gen}', \text{Enc}', \text{Dec}')$ that provably satisfies Weak-1-CPA security but does **not** satisfy Weak-2-CPA security,

1. Define your scheme $(\text{Gen}', \text{Enc}', \text{Dec}')$ and argue that it does not satisfy Weak-2-CPA security. (10 points)

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2. Prove that your scheme satisfies Weak-1-CPA security. (10 points)

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5 Fill in the Blanks (15 points)

1. How many functions are there from $\log_2(n)$ bits to n^2 bits? (5 points)

2. Let $\Pi = (\text{Gen}, \text{Enc}, \text{Dec})$ be a CPA-secure encryption scheme. Construct a CPA-secure encryption scheme Π' that is **not** CCA-secure. Do not use any other cryptographic primitives (e.g. PRG, PRF) in your construction. Provide a brief explanation for why the scheme is not CCA-secure. (5 points)

3. Show that CBC mode encryption is not CCA-secure. (5 points)